## The Krugman model of international trade with process innovation

## Model assumptions

- Countries and goods can be ranked according to their technological level
- An "advanced" country has technological advantages in the production of high-tech goods
- A "TECHNOLOGIC FRONTIER" defines the "state of the art" of technology
- Industries are characterized by different speed of introduction of technological progress
- Industries ranking is stable and is measured on the basis of their time distance from the frontier
- Labour is the only factor of production

Two countries model (1 e 2)

the labour requirement in production of good *z* in country paese *i* is:

$$a_i(z)$$
  $i = 1,2$ 

 $a^*(z)$  is the "best" (lower) labour requirement in production of good z (it defines the "best technology")

labour input (hours) required by the "best technology" continuously decreases through time

$$a^*(z) = \exp\left[-g_z t\right] = e^{-g_z t}$$

 $g_z$  is the growth rate of technological progress in industry Z

Each country has a time lag with respect to the frontier:

$$a_1(z) = \exp\left[-g_z(t - \tau_1)\right]$$

If country 2 has a technological lag with respect to country 1, then:  $\tau_2 > \tau_1$ 

Country I is more efficient in every industry

Productivity advantage is equal to:

$$\frac{a_2(z)}{a_1(z)} = \frac{\exp\left[-g_z(t-\tau_2)\right]}{\exp\left[-g_z(t-\tau_1)\right]} = \exp\left[-g_z(t-\tau_2) + g_z(t-\tau_1)\right]$$

$$\frac{a_2(z)}{a_1(z)} = \exp\left[g_z(\tau_2 - \tau_1)\right]$$

Productivity advantage is increasing in  $g_z$ 

Consumers' demand is identical in the two countries In a continuum of goods ranked in decreasing order of technological efficiency, country 1 productivity advantage is given by

$$A(z) = \frac{a_2(z)}{a_1(z)}$$
  $A'_z > 0$ 

 $\overline{z}$  is the good whose production cost is the same in the countries 1 and 2

$$w_{1}a_{1}(z) = w_{2}a_{2}(z)$$

$$\frac{w_{1}}{w_{2}} = \frac{a_{2}(z)}{a_{1}(z)} = A(\overline{z})$$

Goods  $z < \overline{z}$  are produced (are cheaper) in 2

Goods  $z > \overline{z}$  are produced (are cheaper) in 1

The income share S spent in purchases of goods of country 2 grows with the range of good that are produced in that country:

$$S = S(\overline{z})$$
  $S' > 0$ 

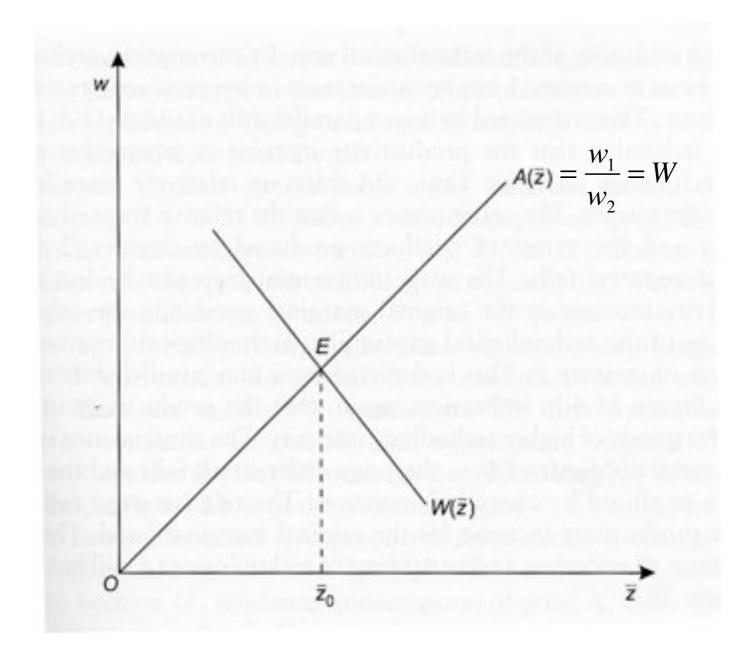
S is the income share of countries I and 2 spent buying goods of country 2 (it is equal)

In equilibrium, the output value of country 2 is equal to world demand:

$$w_1 L_1 S(\overline{z}) + w_2 L_2 S(\overline{z}) = w_2 L_2$$
$$w_1 L_1 S(\overline{z}) = w_2 L_2 \left[ 1 - S(\overline{z}) \right]$$

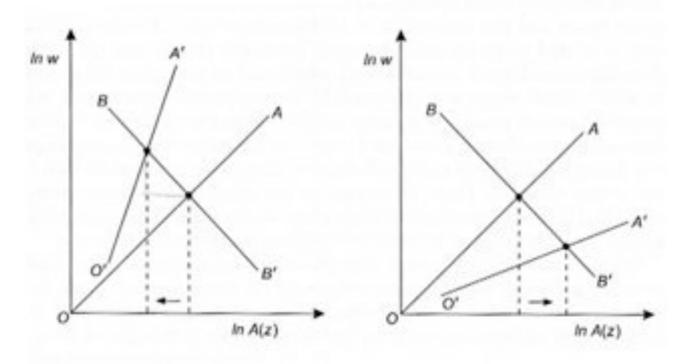
If  $W = \frac{w_1}{w_2}$  is relative wage, then

$$W = \frac{L_2}{L_1} \frac{1 - S(\overline{z})}{S(\overline{z})} \qquad \frac{dW}{d\overline{z}} = \frac{L_2}{L_2} \cdot \frac{-S'(\overline{z})}{\left[S(\overline{z})\right]^2} < 0$$



## Effects of "technological gap" changes

We use a logarithmic version of the model: "Gap" increases "Gap" decreases



- When country I increases its technological advantage, the range of goods produced in country I enlarges
  - Relative wages increases too but *less* than the productivity gap
- If "gap" reduces (catching-up), then we have opposite conclusions.